

What is claimed is:

1. A Montgomery modular multiplier which calculates a value congruent to " $ABR^{-1}$ " (mod  $M$ ), where  $A$  and  $B$  are input  $n$ -bit numbers,  $R^{-1}$  is an inverse number of  $R$  modular-multiplied for "mod  $M$ ", and  $M$  is a modulus, the Montgomery modular multiplier comprising:

an A-register storing a bit value  $a_i$  (where  $i$  is an integer ranging from 0 to  $n-1$ ) of the number  $A$ , which is smaller than the modulus  $M$ ;

a B-register storing a bit value  $b_i$  of the number  $B$ , which is smaller than the modulus  $M$ ;

an M-register storing a bit value  $m_i$  of the modulus  $M$ , which is an odd number;

a  $b_iA$  calculation logic circuit multiplying the number  $A$  by  $b_i$  to obtain  $b_iA$ ;

a  $q_i$  calculation logic circuit solving a Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ", where  $s_0$  is the least significant bit (LSB) of a sum  $S$ ,  $c_0$  is the LSB of a carry  $C$ ,  $b_i$  is the bit value of the number  $B$ , and  $a_0$  is the LSB of the number  $A$ , to obtain a bit value  $q_i$ ;

a  $q_iM$  calculation logic circuit multiplying  $M$  by  $q_i$  to obtain  $q_iM$ ;

a 4-2 compressor first performing  $n$  additions on the carry  $C$ , the sum  $S$ , the  $b_iA$ , and the  $q_iM$  to obtain interim values summing the interim values to obtain a result by carry propagation adder in response to a carry propagation adder signal;

an S-register updating a bit value  $s_i$  of the sum  $S$  and storing the updated bit value; and

a C-register updating a bit value  $c_i$  of the carry  $C$  and storing the updated bit value.

2. The Montgomery modular multiplier of claim 1, wherein the 4-2 compressor comprises:

a first full adder unit, summing a bit value  $b_ia_i$  of  $b_iA$ , a bit value  $s_{i+1}$  of the sum  $S$ , and the bit value  $c_i$  of the carry  $C$  to obtain a carry  $cA_i$  and a sum  $sA_i$ ;

a MUX unit selectively outputting either a bit value  $q_i m_i$  of  $q_i M$ , the carry  $cA_{i-1}$ , and  $sA_i$  or the bit value  $s_{i+1}$  of  $S$ , the bit value  $c_i$  of the carry  $C$ , and the bit value  $c_{i-1}$  of the  $C$ , in response to the carry propagation adder signal;

a second full adder unit performing  $n$  additions on the bit value  $q_i m_i$  of  $q_i M$ ,  $cA_{i-1}$ , and  $sA_i$  to calculate interim bit values  $s_i$  and  $c_i$  of  $S$  and  $C$ , when the carry propagation adder signal is in an inactive state, and then summing the bit value  $s_{i+1}$  of  $S$ , the bit value  $c_i$  of  $C$ , and the bit value  $c_{i-1}$  of  $C$  to obtain final results of the sum  $S$  and carry  $C$ , when the carry propagation adder signal is in an active state.

3. The Montgomery modular multiplier of claim 1, wherein the carry save adder structure is a 4-input 2-output structure, in which the first and second full adder units operate when the carry propagation adder signal is in an inactive state.

4. The Montgomery modular multiplier of claim 1, wherein the carry propagation adder structure is a 3-input 2-output structure, in which only the second full adder unit operates when the carry propagation adder signal is in an active state.

5. The Montgomery modular multiplier of claim 2, wherein the LSB of the carry  $cA_{i-1}$  and the LSB of the carry  $c_{i-1}$  are in a first logic state.

6. The Montgomery modular multiplier of claim 2, wherein the Most Significant Bit (MSB) of the sum  $s_{i+1}$  is equal to the carry  $cA_{n-1}$  at a clock pulse before the carry propagation adder signal is activated.

7. A method of performing a Montgomery modular multiplication in a Montgomery modular multiplier, which includes registers for storing bit values  $a_i$ ,  $b_i$ ,  $m_i$ ,  $c_i$ , and  $s_i$  (where  $i$  denotes an integer in the range of 0 to  $n*1$ ) of a word  $A$ , a word  $B$ , a modulus  $M$ , a carry  $C$ , and a sum  $S$ , respectively, and calculates a value congruent to " $ABR^{-1}$ " (mod  $M$ ), where  $A$  and  $B$  are input  $n$ -bit numbers,  $R^{-1}$  is an inverse number of  $R$  modular-multiplied for "mod  $M$ ", and  $M$  is a modulus, the method comprising:

receiving the number A, the number B, and the modulus M;  
 multiplying the number A by a bit value  $b_i$  to obtain each bit of  $b_iA$ ;  
 solving a Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ", where  $s_0$  is the least significant bit (LSB) of a sum S,  $c_0$  is the LSB of a carry C,  $b_i$  is the bit value of the number B, and  $a_0$  is the LSB of the number A, to obtain a bit value  $q_i$  (where i denotes an integer in the range of 0 to  $n-1$ );  
 multiplying the number M by the bit value  $q_i$  to obtain each bit of  $q_iM$ ;  
 performing n additions on the carry C, the sum S, the  $b_iA$ , and the  $q_iM$  to obtain interim values for each bit of the sum S and the carry C in a carry save adder structure, in response to a carry propagation adder signal; and  
 summing the interim values to obtain the final results of the sum S and carry C in a carry propagation adder structure, in response to the carry propagation adder signal.

8. The method of claim 7, wherein the number A is smaller than the modulus M.

9. The method of claim 7, wherein the number B is smaller than the modulus M.

10. The method of claim 7, wherein the modulus M is an odd number.

11. The method of claim 7, wherein the interim and final values of S and the interim and final values of C are calculated by:

summing a bit value  $b_iA_i$  of the  $b_iA$ , a bit value  $s_{i+1}$  of S, and the bit value  $c_i$  of C to obtain a carry  $cA_i$  and  $sA_i$ ;

selectively outputting either a bit value  $q_iM_i$  of the  $q_iM$ ,  $cA_{i-1}$ , and  $sA_i$  or the bit value  $s_{i+1}$  of S, the bit value  $c_i$  of C, and a bit value  $c_{i-1}$  of C, in response to the carry propagation adder signal;

performing n additions on the bit value  $q_iM_i$  of the  $q_iM$ ,  $cA_{i-1}$ , and  $sA_i$  to calculate interim bit values  $s_i$  and  $c_i$  of S and C, when the carry propagation adder signal is in an inactive state; and

summing the bit value  $s_{i+1}$  of S, the bit value  $c_i$  of C, and the bit value  $c_{i-1}$  of C to obtain final results of S and C, when the carry propagation adder signal is in an active state.

12. The method of claim 7, wherein the carry save adder structure is a 4-input 2-output structure, in which the interim values of S and C are obtained from the  $b_iA$  and  $q_iM$  when the carry propagation adder signal is in an inactive state.

13. The method of claim 7, wherein the carry propagation adder structure is a 3-input 2-output structure, in which the final values of S and C are obtained from the interim values of S and C when the carry propagation adder signal is in an active state.

14. The method of claim 11, wherein the LSB of  $cA_{i-1}$  and the LSB of  $c_{i-1}$  are in a first logic state.

15. The method of claim 11, wherein the MSB value of  $s_{i+1}$  is equal to the bit value  $cA_{n-1}$  at a clock before the carry propagation adder signal is activated.

16. A method of performing radix  $2^N$  Montgomery multiplication, where  $N \geq 1$ , comprising;  
receiving a multiplicand (A), a modulus (M), and a multiplier (B);  
performing carry save addition on at least four inputs related to the multiplicand, modulus, and multiplier to generate a result in redundant representation; and  
performing carry propagation addition to generate a result in normal representation in response to a carry propagation adder signal.

17. A Montgomery multiplier comprising:  
a multiplicand (A) register, storing a bit value  $a_i$  of the number A;  
a modulus (M) register, storing a bit value  $m_i$  of the number M;  
a multiplier (B) register, storing a bit value  $b_i$  of the number B;

a  $b_i A$  calculation logic circuit multiplying the number  $A$  by a bit value  $b_i$  to obtain each bit of  $b_i A$ ;

a  $q_i$  calculation logic circuit solving a Boolean logic equation " $s_0 \text{ XOR } c_0 \text{ XOR } (b_i \text{ AND } a_0)$ ", where  $s_0$  is the least significant bit (LSB) of a sum  $S$ ,  $c_0$  is the LSB of a carry  $C$ ,  $b_i$  is the bit value of the number  $B$ , and  $a_0$  is the LSB of the number  $A$ , to obtain a bit value  $q_i$  (where  $i$  denotes an integer in the range of 0 to  $n-1$ );

a  $q_i M$  calculation logic circuit multiplying the modulus  $M$  by the bit value  $q_i$  to obtain each bit of  $q_i M$ ; and

a t-s compressor, wherein  $t > 3$ , and  $s > 1$ , performing  $n$  additions on the carry  $C$ , the sum  $S$ , the  $b_i A$ , and the  $q_i M$  to obtain interim values for each bit of the sum  $S$  and the carry  $C$  in a carry save adder structure and summing the interim values to obtain final results of the  $S$  and  $C$  in a carry propagation adder structure, in response to a carry propagation adder signal.